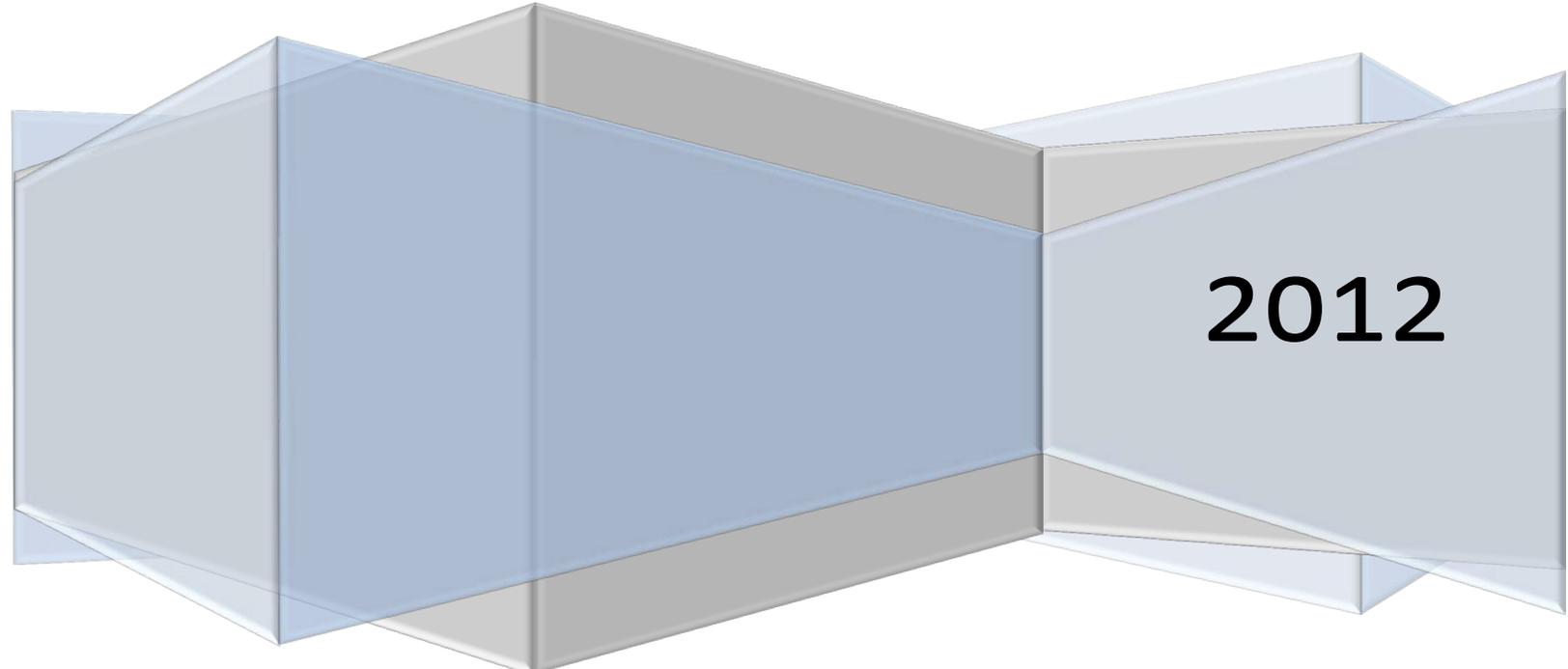


**South Slave Divisional Education Council**

**Math 30-1**  
**Curriculum Package**  
**February 2012**



**2012**

**Strand: Trigonometry**

**General Outcome: Develop trigonometric**

Specific Outcomes	Achievement Indicators – Measurable outcomes
<i>It is expected that students will:</i>	<i>The following set of indicators may be used to assess student achievement for each related specific learning outcome. Students who have fully met the specific learning outcomes are able to:</i>
Demonstrate an understanding of angles in standard position, expressed in degrees and radians.	<ul style="list-style-type: none"> <li>• Sketch, in standard position, an angle (positive or negative) when the measure is given in degrees.</li> <li>• Describe the relationship among different systems of angle measurement, with emphasis on radians and degrees.</li> <li>• Sketch, in standard position, an angle with a measure of 1 radian.</li> <li>• Sketch, in standard position, an angle with a measure expressed in the form <math>k\pi</math> radians, where <math>k \in \mathbb{Q}</math>.</li> <li>• Express the measure of an angle in radians (exact value or decimal approximation), given its measure in degrees.</li> <li>• Express the measure of an angle in degrees, given its measure in radians (exact value or decimal approximation).</li> <li>• Determine the measures, in degrees or radians, of all angles in a given domain that are coterminal with a given angle in standard position.</li> <li>• Determine the general form of the measures, in degrees or radians, of all angles that are coterminal with a given angle in standard position.</li> <li>• Explain the relationship between the radian measure of an angle in standard position and the length of the arc cut on a circle of radius <math>r</math>, and solve problems based upon that relationship.</li> </ul>
Develop and apply the equation of the unit circle.	<ul style="list-style-type: none"> <li>• Derive the equation of the unit circle from the Pythagorean theorem.</li> <li>• Describe the six trigonometric ratios, using a point <math>P(x, y)</math> that is the intersection of the terminal arm of an angle and the unit circle.</li> <li>• Generalize the equation of a circle with centre <math>(0, 0)</math> and radius <math>r</math>.</li> </ul>
Solve problems, using the six trigonometric ratios for angles expressed in radians and degrees.	<ul style="list-style-type: none"> <li>• Determine, with technology, the approximate value of a trigonometric ratio for any angle with a measure expressed in either degrees or radians.</li> <li>• Determine, using a unit circle or reference triangle, the exact value of a trigonometric ratio for angles expressed in degrees that are multiples of <math>0^\circ</math>, <math>30^\circ</math>, <math>45^\circ</math>, <math>60^\circ</math> or <math>90^\circ</math>, or for angles expressed in radians that are multiples of <math>\frac{\pi}{6}</math>, <math>\frac{\pi}{4}</math>, <math>\frac{\pi}{3}</math> or <math>\frac{\pi}{2}</math>, and explain the strategy.</li> <li>• Determine, with or without technology, the measures, in degrees or radians, of the angles in a specified domain, given the value of a trigonometric ratio.</li> <li>• Explain how to determine the exact values of the six trigonometric ratios, given the coordinates of a point on the terminal arm of an angle in standard position.</li> <li>• Determine the measures of the angles in a specified domain in degrees or radians, given a point on the terminal arm of an angle in standard position.</li> <li>• Determine the exact values of the other trigonometric ratios, given the value of one trigonometric ratio in a specified domain.</li> <li>• Sketch a diagram to represent a problem that involves trigonometric ratios.</li> <li>• Solve a problem, using trigonometric ratios.</li> </ul>

**Strand: Trigonometry**

**General Outcome: Develop trigonometric**

Specific Outcomes	Achievement Indicators – Measurable outcomes
<p><i>It is expected that students will:</i></p>	<p><i>The following set of indicators may be used to assess student achievement for each related specific learning outcome. Students who have fully met the specific learning outcomes are able to:</i></p>
<p>Graph and analyze the trigonometric functions sine, cosine and tangent to solve problems.</p>	<ul style="list-style-type: none"> <li>• Sketch, with or without technology, the graph of <math>y = \sin x</math>, <math>y = \cos x</math> or <math>y = \tan x</math>.</li> <li>• Determine the characteristics (amplitude, asymptotes, domain, period, range and zeros) of the graph of <math>y = \sin x</math>, <math>y = \cos x</math> or <math>y = \tan x</math>.</li> <li>• Determine how varying the value of <math>a</math> affects the graphs of <math>y = a \sin x</math> and <math>y = a \cos x</math>.</li> <li>• Determine how varying the value of <math>d</math> affects the graphs of <math>y = \sin x + d</math> and <math>y = \cos x + d</math>.</li> <li>• Determine how varying the value of <math>c</math> affects the graphs of <math>y = \sin(x + c)</math> and <math>y = \cos(x + c)</math>.</li> <li>• Determine how varying the value of <math>b</math> affects graphs of <math>y = \sin bx</math> and <math>y = \cos bx</math>.</li> <li>• Sketch, without technology, graphs of the form <math>y = a \sin b(x - c) + d</math> or <math>y = a \cos b(x - c) + d</math>, using transformations, and explain the strategies.</li> <li>• Determine the characteristics (amplitude, asymptotes, domain, period, phase shift, range and zeros) of the graph of a trigonometric function of the form <math>y = a \sin b(x - c) + d</math> or <math>y = a \cos b(x - c) + d</math>.</li> <li>• Determine the values of <math>a</math>, <math>b</math>, <math>c</math> and <math>d</math> for functions of the form <math>y = a \sin b(x - c) + d</math> or <math>y = a \cos b(x - c) + d</math> that correspond to a given graph, and write the equation of the function.</li> <li>• Determine a trigonometric function that models a situation to solve a problem.</li> <li>• Explain how the characteristics of the graph of a trigonometric function relate to the conditions in a problem situation.</li> <li>• Solve a problem by analyzing the graph of a trigonometric function.</li> </ul>
<p>Solve, algebraically and graphically, first and second degree trigonometric equations with the domain expressed in degrees and radians.</p>	<ul style="list-style-type: none"> <li>• Verify, with or without technology, that a given value is a solution to a trigonometric equation.</li> <li>• Determine, algebraically, the solution of a trigonometric equation, stating the solution in exact form when possible.</li> <li>• Determine, using technology, the approximate solution of a trigonometric equation in a restricted domain.</li> <li>• Relate the general solution of a trigonometric equation to the zeros of the corresponding trigonometric function (restricted to sine and cosine functions).</li> <li>• Determine, using technology, the general solution of a given trigonometric equation.</li> <li>• Identify and correct errors in a solution for a trigonometric equation.</li> </ul>
<p>Prove trigonometric identities, using: reciprocal identities, quotient identities, Pythagorean identities, sum or difference identities (restricted to sine, cosine and tangent), double-angle identities (restricted to sine, cosine and tangent).</p>	<ul style="list-style-type: none"> <li>• Explain the difference between a trigonometric identity and a trigonometric equation.</li> <li>• Verify a trigonometric identity numerically for a given value in either degrees or radians.</li> <li>• Explain why verifying that the two sides of a trigonometric identity are equal for given values is insufficient to conclude that the identity is valid.</li> <li>• Determine, graphically, the potential validity of a trigonometric identity, using technology.</li> <li>• Determine the non-permissible values of a trigonometric identity.</li> <li>• Prove, algebraically, that a trigonometric identity is valid.</li> <li>• Determine, using the sum, difference and double-angle identities, the exact value of a trigonometric ratio.</li> </ul>

**Strand: Relations and Functions**

**General Outcome:** Develop algebraic and graphical reasoning through the study of relations

Specific Outcomes	Achievement Indicators – Measurable outcomes
<i>It is expected that students will:</i>	<i>The following set of indicators may be used to assess student achievement for each related specific learning outcome. Students who have fully met the specific learning outcomes are able to:</i>
Demonstrate an understanding of operations on, and compositions of, functions.	<ul style="list-style-type: none"> <li>• Sketch the graph of a function that is the sum, difference, product or quotient of two functions, given their graphs.</li> <li>• Write the equation of a function that is the sum, difference, product or quotient of two or more functions, given their equations.</li> <li>• Determine the domain and range of a function that is the sum, difference, product or quotient of two functions.</li> <li>• Write a function <math>h(x)</math> as the sum, difference, product or quotient of two or more functions.</li> <li>• Determine the value of the composition of functions when evaluated at a point, including: <math>f(f(a))</math>, <math>f(g(a))</math>, <math>g(f(a))</math>.</li> <li>• Determine, given the equations of two functions <math>f(x)</math> and <math>g(x)</math>, the equation of the composite function: <math>f(f(x))</math>, <math>f(g(x))</math>, <math>g(f(x))</math> and explain any restrictions.</li> <li>• Sketch, given the equations of two functions <math>f(x)</math> and <math>g(x)</math>, the graph of the composite function: <math>f(f(x))</math>, <math>f(g(x))</math>, <math>g(f(x))</math></li> <li>• Write a function <math>h(x)</math> as the composition of two or more functions.</li> <li>• Write a function <math>h(x)</math> by combining two or more functions through operations on, and compositions of, functions.</li> </ul>
Demonstrate an understanding of the effects of horizontal and vertical translations on the graphs of functions and their related equations.	<ul style="list-style-type: none"> <li>• Compare the graphs of a set of functions of the form <math>y - k = f(x)</math> to the graph of <math>y = f(x)</math>, and generalize, using inductive reasoning, a rule about the effect of <math>k</math>.</li> <li>• Compare the graphs of a set of functions of the form <math>y = f(x - h)</math> to the graph of <math>y = f(x)</math>, and generalize, using inductive reasoning, a rule about the effect of <math>h</math>.</li> <li>• Compare the graphs of a set of functions of the form <math>y - k = f(x - h)</math> to the graph of <math>y = f(x)</math>, and generalize, using inductive reasoning, a rule about the effects of <math>h</math> and <math>k</math>.</li> <li>• Sketch the graph of <math>y - k = f(x)</math>, <math>y = f(x - h)</math> or <math>y - k = f(x - h)</math> for given values of <math>h</math> and <math>k</math>, given a sketch of the function <math>y = f(x)</math>, where the equation of <math>y = f(x)</math> is not given.</li> <li>• Write the equation of a function whose graph is a vertical and/or horizontal translation of the graph of the function <math>y = f(x)</math>.</li> </ul>
Demonstrate an understanding of the effects of horizontal and vertical stretches on the graphs of functions and their related equations.	<ul style="list-style-type: none"> <li>• Compare the graphs of a set of functions of the form <math>y = af(x)</math> to the graph of <math>y = f(x)</math>, and generalize, using inductive reasoning, a rule about the effect of <math>a</math>.</li> <li>• Compare the graphs of a set of functions of the form <math>y = f(bx)</math> to the graph of <math>y = f(x)</math>, and generalize, using inductive reasoning, a rule about the effect of <math>b</math>.</li> <li>• Compare the graphs of a set of functions of the form <math>y = af(bx)</math> to the graph of <math>y = f(x)</math>, and generalize, using inductive reasoning, a rule about the effects of <math>a</math> and <math>b</math>.</li> <li>• Sketch the graph of <math>y = af(x)</math>, <math>y = f(bx)</math> or <math>y = af(bx)</math> for given values of <math>a</math> and <math>b</math>, given a sketch of the function <math>y = f(x)</math>, where the equation of <math>y = f(x)</math> is not given.</li> <li>• Write the equation of a function, given its graph which is a vertical and/or horizontal stretch of the graph of the function <math>y = f(x)</math>.</li> </ul>
Apply translations and stretches to the graphs and equations of functions.	<ul style="list-style-type: none"> <li>• Sketch the graph of the function <math>y - k = af(b(x - h))</math> for given values of <math>a</math>, <math>b</math>, <math>h</math> and <math>k</math>, given the graph of the function <math>y = f(x)</math>, where the equation of <math>y = f(x)</math> is not given.</li> <li>• Write the equation of a function, given its graph which is a translation and/or stretch of the graph of the function <math>y = f(x)</math>.</li> </ul>

**Strand: Relations and Functions**

**General Outcome:** Develop algebraic and graphical reasoning through the study of relations

Specific Outcomes	Achievement Indicators – Measurable outcomes
<i>It is expected that students will:</i>	<i>The following set of indicators may be used to assess student achievement for each related specific learning outcome. Students who have fully met the specific learning outcomes are able to:</i>
Demonstrate an understanding of the effects of reflections on the graphs of functions and their related equations, including reflections through the: x-axis, y-axis, line $y = x$ .	<ul style="list-style-type: none"> <li>• Generalize the relationship between the coordinates of an ordered pair and the coordinates of the corresponding ordered pair that results from a reflection through the x-axis, the y-axis or the line <math>y = x</math>.</li> <li>• Sketch the reflection of the graph of a function <math>y = f(x)</math> through the x-axis, the y-axis or the line <math>y = x</math>, given the graph of the function <math>y = f(x)</math>, where the equation of <math>y = f(x)</math> is not given.</li> <li>• Generalize, using inductive reasoning, and explain rules for the reflection of the graph of the function <math>y = f(x)</math> through the x-axis, the y-axis or the line <math>y = x</math>.</li> <li>• Sketch the graphs of the functions <math>y = -f(x)</math>, <math>y = f(-x)</math> and <math>x = -f(y)</math>, given the graph of the function <math>y = f(x)</math>, where the equation of <math>y = f(x)</math> is not given.</li> <li>• Write the equation of a function, given its graph which is a reflection of the graph of the function <math>y = f(x)</math> through the x-axis, the y-axis or the line <math>y = x</math>.</li> </ul>
Demonstrate an understanding of inverses of relations.	<ul style="list-style-type: none"> <li>• Explain how the graph of the line <math>y = x</math> can be used to sketch the inverse of a relation.</li> <li>• Explain how the transformation <math>(x, y) \Rightarrow (y, x)</math> can be used to sketch the inverse of a relation.</li> <li>• Sketch the graph of the inverse relation, given the graph of a relation.</li> <li>• Determine if a relation and its inverse are functions.</li> <li>• Determine restrictions on the domain of a function in order for its inverse to be a function.</li> <li>• Determine the equation and sketch the graph of the inverse relation, given the equation of a linear or quadratic relation.</li> <li>• Explain the relationship between the domains and ranges of a relation and its inverse.</li> <li>• Determine, algebraically or graphically, if two functions are inverses of each other.</li> </ul>
Demonstrate an understanding of logarithms.	<ul style="list-style-type: none"> <li>• Explain the relationship between logarithms and exponents.</li> <li>• Express a logarithmic expression as an exponential expression and vice versa.</li> <li>• Determine, without technology, the exact value of a logarithm, such as <math>\log_2 8</math>.</li> <li>• Estimate the value of a logarithm, using benchmarks, and explain the reasoning; e.g., since <math>\log_2 8 = 3</math> and <math>\log_2 16 = 4</math>, <math>\log_2 9</math> is approximately equal to 3.1.</li> </ul>
Demonstrate an understanding of the product, quotient and power laws of logarithms.	<ul style="list-style-type: none"> <li>• Develop and generalize the laws for logarithms, using numeric examples and exponent laws.</li> <li>• Derive each law of logarithms.</li> <li>• Determine, using the laws of logarithms, an equivalent expression for a logarithmic expression.</li> <li>• Determine, with technology, the approximate value of a logarithmic expression, such as <math>\log_2 9</math>.</li> </ul>

**Strand: Relations and Functions**

**General Outcome:** Develop algebraic and graphical reasoning through the study of relations

Specific Outcomes	Achievement Indicators – Measurable outcomes
<p><i>It is expected that students will:</i></p>	<p><i>The following set of indicators may be used to assess student achievement for each related specific learning outcome. Students who have fully met the specific learning outcomes are able to:</i></p>
<p>Graph and analyze exponential and logarithmic functions.</p>	<ul style="list-style-type: none"> <li>• Sketch, with or without technology, a graph of an exponential function of the form <math>y = ax</math>, <math>a &gt; 0</math>.</li> <li>• Identify the characteristics of the graph of an exponential function of the form <math>y = ax</math>, <math>a &gt; 0</math>, including the domain, range, horizontal asymptote and intercepts, and explain the significance of the horizontal asymptote.</li> <li>• Sketch the graph of an exponential function by applying a set of transformations to the graph of <math>y = ax</math>, <math>a &gt; 0</math>, and state the characteristics of the graph.</li> <li>• Sketch, with or without technology, the graph of a logarithmic function of the form <math>y = \log_b x</math>, <math>b &gt; 1</math>.</li> <li>• Identify the characteristics of the graph of a logarithmic function of the form <math>y = \log_b x</math>, <math>b &gt; 1</math>, including the domain, range, vertical asymptote and intercepts, and explain the significance of the vertical asymptote.</li> <li>• Sketch the graph of a logarithmic function by applying a set of transformations to the graph of <math>y = \log_b x</math>, <math>b &gt; 1</math>, and state the characteristics of the graph.</li> <li>• Demonstrate, graphically, that a logarithmic function and an exponential function with the same base are inverses of each other.</li> </ul>
<p>Solve problems that involve exponential and logarithmic equations.</p>	<ul style="list-style-type: none"> <li>• Determine the solution of an exponential equation in which the bases are powers of one another.</li> <li>• Determine the solution of an exponential equation in which the bases are not powers of one another, using a variety of strategies.</li> <li>• Determine the solution of a logarithmic equation, and verify the solution.</li> <li>• Explain why a value obtained in solving a logarithmic equation may be extraneous.</li> <li>• Solve a problem that involves exponential growth or decay.</li> <li>• Solve a problem that involves the application of exponential equations to loans, mortgages and investments.</li> <li>• Solve a problem that involves logarithmic scales, such as the Richter scale and the pH scale.</li> <li>• Solve a problem by modelling a situation with an exponential or a logarithmic equation.</li> </ul>
<p>Demonstrate an understanding of factoring polynomials of degree greater than 2 (limited to polynomials of degree <math>\leq 5</math> with integral coefficients).</p>	<ul style="list-style-type: none"> <li>• Explain how long division of a polynomial expression by a binomial expression of the form <math>x - a</math>, <math>a \in I</math>, is related to synthetic division.</li> <li>• Divide a polynomial expression by a binomial expression of the form <math>x - a</math>, <math>a \in I</math>, using long division or synthetic division.</li> <li>• Explain the relationship between the linear factors of a polynomial expression and the zeros of the corresponding polynomial function.</li> <li>• Explain the relationship between the remainder when a polynomial expression is divided by <math>x - a</math>, <math>a \in I</math>, and the value of the polynomial expression at <math>x = a</math> (remainder theorem).</li> <li>• Explain and apply the factor theorem to express a polynomial expression as a product of factors.</li> </ul>

**Strand: Relations and Functions**

**General Outcome:** Develop algebraic and graphical reasoning through the study of relations

Specific Outcomes	Achievement Indicators – Measurable outcomes
<i>It is expected that students will:</i>	<i>The following set of indicators may be used to assess student achievement for each related specific learning outcome. Students who have fully met the specific learning outcomes are able to:</i>
Graph and analyze polynomial functions (limited to polynomial functions of degree $\leq 5$ ).	<ul style="list-style-type: none"> <li>• Identify the polynomial functions in a set of functions, and explain the reasoning.</li> <li>• Explain the role of the constant term and leading coefficient in the equation of a polynomial function with respect to the graph of the function.</li> <li>• Generalize rules for graphing polynomial functions of odd or even degree.</li> <li>• Explain the relationship between: the zeros of a polynomial function, the roots of the corresponding polynomial equation, the x-intercepts of the graph of the polynomial function.</li> <li>• Explain how the multiplicity of a zero of a polynomial function affects the graph.</li> <li>• Sketch, with or without technology, the graph of a polynomial function.</li> <li>• Solve a problem by modelling a given situation with a polynomial function and analyzing the graph of the function.</li> </ul>
Graph and analyze radical functions (limited to functions involving one radical).	<ul style="list-style-type: none"> <li>• Sketch the graph of the function <math>y = \sqrt{x}</math>, using a table of values, and state the domain and range.</li> <li>• Sketch the graph of the function <math>y - k = a\sqrt{b(x - h)}</math> by applying transformations to the graph of the function <math>y = \sqrt{x}</math>, and state the domain and range.</li> <li>• Sketch the graph of the function <math>y = \sqrt{f(x)}</math>, given the graph of the function <math>y = f(x)</math>, and explain the strategies used.</li> <li>• Compare the domain and range of the function <math>y = \sqrt{f(x)}</math>, to the domain and range of the function <math>y = f(x)</math>, and explain why the domains and ranges may differ.</li> <li>• Describe the relationship between the roots of a radical equation and the x-intercepts of the graph of the corresponding radical function.</li> <li>• Determine, graphically, an approximate solution of a radical equation.</li> </ul>
Graph and analyze rational functions (limited to numerators and denominators that are monomials, binomials or trinomials).	<ul style="list-style-type: none"> <li>• Graph, with or without technology, a rational function.</li> <li>• Analyze the graphs of a set of rational functions to identify common characteristics.</li> <li>• Explain the behaviour of the graph of a rational function for values of the variable near a non-permissible value.</li> <li>• Determine if the graph of a rational function will have an asymptote or a hole for a non-permissible value.</li> <li>• Match a set of rational functions to their graphs, and explain the reasoning.</li> <li>• Describe the relationship between the roots of a rational equation and the x-intercepts of the graph of the corresponding rational function.</li> <li>• Determine, graphically, an approximate solution of a rational equation.</li> </ul>

**Strand:** Permutations, Combinations & Binomial Theorem

**General Outcome:** Develop algebraic and numeric reasoning that involves combinatorics.

Specific Outcomes	Achievement Indicators – Measurable outcomes
<i>It is expected that students will:</i>	<i>The following set of indicators may be used to assess student achievement for each related specific learning outcome. Students who have fully met the specific learning outcomes are able to:</i>
Apply the fundamental counting principle to solve problems.	<ul style="list-style-type: none"> <li>• Count the total number of possible choices that can be made, using graphic organizers such as lists and tree diagrams.</li> <li>• Explain, using examples, why the total number of possible choices is found by multiplying rather than adding the number of ways the individual choices can be made.</li> <li>• Solve a simple counting problem by applying the fundamental counting principle.</li> </ul>
Determine the number of permutations of $n$ elements taken $r$ at a time to solve problems.	<ul style="list-style-type: none"> <li>• Count, using graphic organizers such as lists and tree diagrams, the number of ways of arranging the elements of a set in a row.</li> <li>• Determine, in factorial notation, the number of permutations of <math>n</math> different elements taken <math>n</math> at a time to solve a problem.</li> <li>• Determine, using a variety of strategies, the number of permutations of <math>n</math> different elements taken <math>r</math> at a time to solve a problem.</li> <li>• Explain why <math>n</math> must be greater than or equal to <math>r</math> in the notation <math>nPr</math>.</li> <li>• Solve an equation that involves <math>nPr</math> notation, such as <math>nP2 = 30</math>.</li> <li>• Explain, using examples, the effect on the total number of permutations when two or more elements are identical.</li> </ul>
Determine the number of combinations of $n$ different elements taken $r$ at a time to solve problems.	<ul style="list-style-type: none"> <li>• Explain, using examples, the difference between a permutation and a combination.</li> <li>• Determine the number of ways that a subset of <math>k</math> elements can be selected from a set of <math>n</math> different elements.</li> <li>• Determine the number of combinations of <math>n</math> different elements taken <math>r</math> at a time to solve a problem.</li> <li>• Explain why <math>n</math> must be greater than or equal to <math>r</math> in the notation <math>nCr</math> or <math>\binom{n}{r}</math>.</li> <li>• Explain, using examples, why <math>nCr = nCn-r</math> or <math>\binom{n}{r} = \binom{n}{n-r}</math>.</li> <li>• Solve an equation that involves <math>nCr</math> or <math>\binom{n}{r}</math> notation, such as <math>nC2 = 15</math> or <math>\binom{n}{2} = 15</math>.</li> </ul>
Expand powers of a binomial in a variety of ways, including using the binomial theorem (restricted to exponents that are natural numbers).	<ul style="list-style-type: none"> <li>• Explain the patterns found in the expanded form of <math>(x + y)^n</math>, <math>n \leq 4</math> and <math>n \in \mathbb{N}</math>, by multiplying <math>n</math> factors of <math>(x + y)</math>.</li> <li>• Explain how to determine the subsequent row in Pascal's triangle, given any row.</li> <li>• Relate the coefficients of the terms in the expansion of <math>(x + y)^n</math> to the <math>(n + 1)</math> row in Pascal's triangle.</li> <li>• Explain, using examples, how the coefficients of the terms in the expansion of <math>(x + y)^n</math> are determined by combinations.</li> <li>• Expand, using the binomial theorem, <math>(x + y)^n</math>.</li> <li>• Determine a specific term in the expansion of <math>(x + y)^n</math>.</li> </ul>